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# Analyzing Pharmaceutical Compounds Through Neutrosophic Over Soft Hyperconnected Spaces

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# ABSTRACT

Correlation is crucial in the decision-making approach. The foundational concepts of neutrosophic sets and topological spaces within the context of a basic environment is given. It introduces and explores innovative concepts such as neutrosophic over soft semi-j open sets and neutrosophic over soft hyperconnected spaces. Through a numerical illustration, the manuscript demonstrates the application of these concepts to determine the most effective method for a novel pharmaceutical application using a neutrosophic over soft measure of correlation. The findings highlight the practical utility and potential of these new theoretical constructs in enhancing decision-making processes within the pharmaceutical industry.

Keywords: Neutrosophic Over Soft Topological Space, Neutrosophic Over Soft open set, Neutrosophic Over Soft Connected Space, Neutrosophic Over Soft Hyperconnected Space and Neutrosophic Over Soft Extremely Disconnected.

## INTRODUCTION

Uncertainty influences many facets of daily life, from the randomness of rolling dice to the unpredictability of flipping a coin on an uneven surface. These scenarios illustrate the fundamental nature of uncertainty, prompting the development of mathematical frameworks to address such variability. In 1965, Zadeh<sup>24</sup> introduced fuzzy sets, marking a significant milestone in mathematical theory by presenting the concept of membership degrees to model uncertainty. Zadeh also laid the groundwork for possibility theory<sup>25</sup>, broadening the scope of how

uncertainties could be conceptualized and managed. Building upon Zadeh's contributions, Bellman *et al.*,<sup>4</sup> explored decision-making under uncertainty, further solidifying the practical implications of fuzzy logic.

By introducing intuitionistic fuzzy sets, Atanassov<sup>2</sup> provided a more comprehensive framework for representing uncertain information. These sets consider degrees of membership, non-membership, and hesitation, extending fuzzy set theory to capture uncertainty more effectively.

The introduction of neutrosophic sets

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by Smarandache<sup>20</sup> represented another leap forward, introducing a novel approach to handling uncertainty that goes beyond traditional fuzzy and intuitionistic models. Neutrosophic sets allow for the representation of indeterminate, contradictory, and uncertain information, offering versatile applications across diverse fields.

Christianto<sup>6</sup> proposed various utilities for neutrosophic sets, highlighting their potential in modeling complex and ambiguous information scenarios. Meanwhile, Molodtsov<sup>16</sup> introduced soft sets in 1999, which provide a mechanism to handle uncertainties in a set-theoretic context. Maji *et al.*,<sup>15</sup> subsequently advanced soft set theory, demonstrating its effectiveness in practical applications.

The concept of neutrosophic soft sets, introduced by Broumi<sup>5</sup> in 2002, combines the flexibility of neutrosophic sets with the simplicity of soft sets, enhancing their applicability in decisionmaking and problem-solving.

Smarandache introduced Neutrosophic Overset, Neutrosophic Underset, and Neutrosophic Offset in the year 2016<sup>20</sup> Smarandache's innovative contributions continued with the introduction of plithogenic sets and logic in 2017<sup>22</sup>, offering new insights into handling uncertainties involving contradictory or paradoxical information. This concept has since garnered significant attention and further exploration<sup>23,9</sup> RN Devi and Y Parthiban introduced a novel concept of Neutrosophic Pythagorean Plithogenic Hypersoft Set Approach to School Selection With TOPSIS Method stimulating research efforts into its theoretical underpinnings and practical implications<sup>7,8,17,13,14,18</sup>.

A notable advancement in this field is the elucidation of Plithogenic Hypersoft Sets within a Fuzzy Neutrosophic Environment by Rayees *et al.*,<sup>3</sup>, underscoring the continued evolution and integration of these theories to address complex real-world problems<sup>1,11,12</sup>.

This manuscript clearly expain the basic definitions for neutrosophic set and topological space. By inovating a concept neutrosophic over soft semi-j open set and neutrosophic over soft hyperconnected space. An numerical illustration is given to determine the most effective one for a new pharmaceutical application using neutrosophic over soft measure of correlation.

### Preliminaries

This section introduces the basic definitions of Neutrosophic Set  $(NS)^{20}$ , Neutrosophic Over Soft Topological Space, Neutrosophic Over Set  $(NOS)^{21}$ , and Neutrosophic Over Soft Set  $(N_c^{\circ}-set)$ .

**Definition 1** <sup>8</sup>An N<sub>s</sub><sup>o</sup>-set is defined as a valued function from the set of parameters E on a non-empty set H. This is expressed as:

$$\begin{split} J &= (\lambda N_s^{\circ}), \, \epsilon) = \{ (e, \, \{m, \, \vartheta_J(m), \, \tilde{\partial}_J(m), \, \tilde{\partial}_J(m) \, \gamma_J(m) \colon m \\ &\in H \} ) \colon e \, \in \, \epsilon \} \end{split}$$

The set-valued function defining the  $\rm N_{s}^{\,o}\text{-set}$  is given by:

 $\lambda N_{s}^{\circ}$ ):  $\varepsilon \rightarrow \rho(H)$ 

Where  $\rho(H)$  represents the set of all  $N_{_{S}}^{\,\,\circ}\text{-set}$  on H.

 $\begin{array}{l} \textbf{Definition } 2^{s}An \ N_{s}^{\circ}\text{-set} \bigcirc = \{e, \{m, 0, 0, \Omega: m \in H\}: e \in \epsilon\} \ \text{is referred to as a Null } N_{s}^{\circ}\text{-set, and} \\ \textcircled{\$} = \{e, \{m, \Omega, \Omega, \Omega, 0: m \in H\}: e \in \epsilon\} \ \text{is referred to as a universal } N_{s}^{\circ}\text{-set.} \end{array}$ 

**Definition 3**<sup>8</sup> Let  $\tau N_s^{\circ}$ ) be a  $N_s^{\circ}$  topology in the  $N_s^{\circ}$ -set J, which is a collection of subsets of an non-empty set H. The pair (H,  $\tau N_s^{\circ}$ ) is called an  $N_s^{\circ}$  topological space if it satify the following conditions:

(i)  $\bigcirc$ ,  $\circledast \in \tau N_s^{\circ}$ .

- (iii) A finite intersection of sets in  $\tau N_s^{o}$  belongs to  $\tau N_s^{o}$ .

In this context, an element of  $\tau N_s^{\circ}$  is referred to as an  $N_s^{\circ}$  open set and compliment of a set  $\tau N_s^{\circ}$  is referred to as an  $N_s^{\circ}$  closed set.

 $\begin{array}{l} \textbf{Definition } 4^{\text{s}} \text{ The operators for the } N_{s}^{\circ} \\ \text{topological interior and closure are defined as int } N_{s}^{\circ} \\ (\text{R}) \text{ and cl } N_{s}^{\circ} (\text{R}), \text{ respectively for all } \text{R} \in (\text{H}, \tau N_{s}^{\circ}). \\ \text{int} N_{s}^{\circ} (\text{R}) = \text{U} \left\{ N: N \subseteq \text{H} \text{ and } N \in \tau N_{s}^{\circ} \right\} \text{ and cl } N_{s}^{\circ} (\text{R}) \\ \Omega = \{ O: \text{H} \subseteq \text{O} \text{ and } O \in \tau N_{s}^{\circ \circ \rho} \}. \end{array}$ 

Neutrosophic Over Soft j-Open Set and Neutrosophic Over Soft Hyperconnected Space

In this part an introduction for  $N_s^{\circ}\beta$  open set,  $N_s^{\circ}$  Connected Space,  $N_s^{\circ}$  Hyperconnected Space and  $N_s^{\circ}$  Extremely Disconnected. Additionally, some of its fundamental properties are examined.

 $\begin{array}{l} \textbf{Definition 5 An N_s^{\circ}-set J in (H,\tau N_s^{\circ}). Then} \\ J \text{ is said to be } N_s^{\circ} \beta \text{ open set } (N_s^{\circ}-\beta \text{ open set}) \text{ of } X \text{ if} \\ \text{ and only if } J \subseteq cl N_s^{\circ} (\text{int } N_s^{\circ} (cl N_s^{\circ} (J))) \end{array}$ 

**Theorem 3.1** Let Jα, where  $\alpha = 1, 2, 3...$ be a collection of N<sub>s</sub><sup>o</sup>-β open set in (H,τN<sub>s</sub><sup>o</sup>). Then UJα is also N<sub>s</sub><sup>o</sup>-β open set in (H, τ(N<sub>s</sub><sup>o</sup>).

Proof. Since  $J\alpha$  is a  $N_s^{\circ}$ - $\beta$  open set in  $(H,\tau(N_s^{\circ})$ . Then  $J\alpha \subseteq cl N_s^{\circ}$  (int  $N_s^{\circ}$  (cl  $N_s^{\circ}$ ) ( $J\alpha$ ). U $J\alpha \subseteq U$  (cl  $N_s^{\circ}$  (int  $N_s^{\circ}$  (cl  $N_s^{\circ}$ ) ( $J) \subseteq cl N_s^{\circ}$  (int  $N_s^{\circ}$  (cl  $N_s^{\circ}$  (U $J\alpha$ ). Hence UJ $\alpha$  is also  $N_s^{\circ}$ - $\beta$  open set in  $(H, \tau N_s^{\circ})$ .

**Theorem 3.2** Let Jα, where = 1, 2, 3... be a collection of N<sub>s</sub><sup>o</sup>-β open set in (H,τN<sub>s</sub><sup>o</sup>). Then ∩Jα is also N<sub>s</sub><sup>o</sup>-β open set in (H,τN<sub>s</sub><sup>o</sup>).

Proof. Since  $J\alpha$  is a  $N_s^{\circ}$ - $\beta$  open set in (H,  $\tau N_s^{\circ}$ . Then  $J\alpha \supseteq cl N_s^{\circ}$  (int  $N_s^{\circ}(clN_s^{\circ} (J\alpha). \cap J\alpha \supseteq \cap$ ( $clN_s^{\circ}$  (int $N_s^{\circ}$ ) (cl  $N_s^{\circ}$ ) (J) cl  $N_s^{\circ}$  (int $N_s^{\circ}$  (cl  $N_s^{\circ} (\cap J\alpha)$ . Hence  $J\alpha$  is also  $N_s^{\circ}$ - $\beta$  open set in (H, $\tau N_s^{\circ}$ ).

**Theorem 3.3** In the space  $(H, \tau N_s^{\circ})$ , every  $N_s^{\circ}$ - $\beta$  open set is a neutrosophic open set. Proof. The proof is obvious.

**Theorem 3.4** Let J be a  $N_s^{\circ}$ - $\beta$  open set in an  $N_s^{\circ}$ -topological space (H,  $\tau N_s^{\circ}$ ), and suppose J  $\subseteq W \subseteq cl N_s^{\circ}$ ) (J). Then, in (H, $\tau N_s^{\circ}$ ), Q is also a  $N_s^{\circ}$ - $\beta$ open set.

 $\begin{array}{l} \label{eq:stars} Proof. \ As \ J \ is \ N_s^{\ o}{\rm -}\beta \ open \ set \ in \ (H,\tau \ N_s^{\ o}). \\ Then \ J \ \sqsubseteq \ cl \ N_s^{\ o} \ (int \ N_s^{\ o} \ (cl \ N_s^{\ o}) \ (J) \ \sqsubseteq \ cl \ N_s^{\ o} \ (J) \ \sqsubseteq \ cl \ N_s^{\ o} \ (J) \ \sqsubseteq \ cl \ N_s^{\ o} \ (int \ N_s^{\ o} \ (cl \ N_s^{\ o}) \ (J))). \\ cl \ N_s^{\ o} \ (int \ N_s^{\ o} \ (cl \ N_s^{\ o}) \ (J) \ \bigsqcup \ cl \ N_s^{\ o} \ (J) \ \bigsqcup \ cl \ N_s^{\ o} \ (int \ N_s^{\ o} \ (lnt \ N_s^{\ o} \ ($ 

**Definition 6** A  $N_s^{\circ}$  in  $(H, \tau N_s^{\circ})$  is said to be proper, if it is neither  $\bigcirc$  nor  $\circledast$ .

**Definition 7** A N<sub>s</sub>°-topological space said to be N<sub>s</sub>°-connected, if it has no proper N<sub>s</sub>°-clopen set. N<sub>s</sub>°-topological space is not a N<sub>s</sub>°-connected then it is disconnected.

**Theorem 3.5** A N<sub>s</sub>°-topological space said to be N<sub>s</sub>°-connected if and only if it doesn't have any N<sub>s</sub>°-open sets J and W providing that  $\vartheta_J(m) = \gamma_W(m)$ ,  $\gamma_J(m) = \vartheta_W(m)$  and  $\tilde{\mathfrak{O}}_J(m) = \tilde{\mathfrak{O}}_W(m)$ .

Proof. Suppose there exist N<sub>s</sub><sup>o</sup>-open sets J and W providing that  $\vartheta_J(m) = \gamma_W(m), \gamma_J(m) = \vartheta_W(m)$  and  $\tilde{\vartheta}_J(m) = \tilde{\vartheta}_W(m)$ 

Then J and W are  $N_s^{\circ}$ -clopen sets in  $(H, \tau N_s^{\circ})$ .  $(H, \tau N_s^{\circ})$  is not  $N_s^{\circ}$ -connected.  $(H, \tau N_s^{\circ})$  is  $N_s^{\circ}$ -connected.

Conversely, assume that (H,  $\tau N_s^{\circ}$ ) is  $N_s^{\circ}$ connected. Then it has a proper  $N_s^{\circ}$ -clopen sets J.  $J^{\wp}$  is a  $N_s^{\circ}$ -open set in (H,  $\tau N_s^{\circ}$ ) say  $J^{\wp} = W$ .  $\vartheta_J(m) = \gamma_w(m)$ ,  $\gamma_J(m) = \vartheta_w(m)$ ,  $\Omega - \delta_J(m) = \Omega - \delta_w(m)$  $- \delta_J(m) = - \delta_w(m)$  $\delta_J(m) = \delta_w(m)$ 

**Theorem 3.6** A N<sub>s</sub><sup>o</sup>-topological space said to be N<sub>s</sub><sup>o</sup>-connected if and only if it doesn't have any N<sub>s</sub><sup>o</sup>-open sets J and W providing that  $\vartheta_J(m) = \gamma_W^{\wp}(m)$ ,  $(m), \gamma_J(m) = \vartheta_W^{\wp}(m)$  and  $\vartheta_J(m) = \vartheta_W^{\wp}(m)$ .

Proof. Directly derived from Theorem 3.5, the proof follows.

Definition 8 An  $N_s^{\,\,o}\text{-set}$  J in  $(H,\tau\,\,N_s^{\,\,o})$  is called

(i)  $N_{\circ}^{\circ}$  Dense( $N_{\circ}^{\circ}$ -Dense) if cl  $N_{\circ}^{\circ}$  (J) = ().

(ii)  $N_s^{\circ}$  Nowhere Dense( $N_s^{\circ}$ -NDense) if int(cl  $N_s^{\circ}$ ) (J)) =  $\bigcirc$ .

**Definition 9** An N<sub>s</sub><sup>o</sup> hyperconnected space is defined as an N<sub>s</sub><sup>o</sup>-topological space (H, $\tau$  N<sub>s</sub><sup>o</sup>), in which every non empty N<sub>s</sub><sup>o</sup>-open subset of (H, $\tau$  N<sub>s</sub><sup>o</sup>) is N<sub>s</sub><sup>o</sup>-dense in (H, $\tau$  N<sub>s</sub><sub>o</sub>).

 $\begin{array}{l} \textbf{Example 1 Let } \epsilon = \{e\} \ be \ a \ set \ of \ parameter \\ on \ H, \ where \ H = \{s_1, s_2\} \ with \ \tau N_s^\circ \ ) = \{\bigcirc, \ \circledast, \ P_1, \ P_2, \ P_3\}. \\ P_1 = \{(e, \{s_1, 1.2, 0.4, 0.3, s_2, 1.3, 0.1, 0.2; s_1, s_2 \in H\}) : e \in \epsilon\} \\ P_2 = \{(e, \{s_1, 1.1, 0.2, 0.1, s_2, 1.2, 0.2, 0.4; s_1, s_2 \in H\}) : e \in \epsilon\} \\ P_3 = \{(e, \{s_1, 1.02, \ 0.14, 0.3, s_2, \ 1.1, \ 0.41, \ 0.22; \ s_1, \ s_2 \in H\}) : e \in \epsilon\} \end{array}$ 

Here every non empty  $N_s^{\circ}$ -open sets  $(\)$ ,  $P_1, P_2, P_3$  are  $N_s^{\circ}$ -Dense in H that is cl  $N_s^{\circ}(P_1) = (\)$ cl  $N_s^{\circ}(P_2) = (\)$ cl  $N_s^{\circ}(P_3) = (\)$ cl  $N_s^{\circ}((\)) = (\)$ cl  $N_s^{\circ}(\) = (\)$ 

Theorem 3.7 Let  $(H, \tau N_s^{\circ})$  be an  $N_s^{\circ}$ -topological space. Then the following properties are equivalent.

(i)  $(H,\tau N_s^{\circ})$  is  $N_s^{\circ}$ -hyperconnected.

(ii) In (H,  $\tau N_s^{\circ}$ ), the only  $N_s^{\circ}$ -open sets are  $\bigcirc$  and  $\circledast$ . Proof. (i)  $\rightarrow$  (ii)

Let  $(H,\tau N_s^{\circ})$  is  $N_s^{\circ}$ -hyperconnected. If J is a  $N_s^{\circ}$ - open set, then by the definition  $J = int N_s^{\circ}$  (cl  $N_s^{\circ}(P)$ ).

 $(\operatorname{int} \operatorname{N}_{\operatorname{s}}^{\circ}(\operatorname{Cl}\operatorname{N}_{\operatorname{s}}^{\circ}(\mathsf{P})^{\wp} = (\circledast \operatorname{-int}\operatorname{N}_{\operatorname{so}}(\operatorname{Cl}\operatorname{N}_{\operatorname{s}}^{\circ}(\mathsf{P})) = \operatorname{cl}\operatorname{N}_{\operatorname{s}}^{\circ}) (\circledast \operatorname{-cl}\operatorname{N}_{\operatorname{s}}^{\circ}(\mathsf{J})) = \operatorname{cl}\operatorname{N}_{\operatorname{so}}(\mathsf{J}^{\wp}) = \operatorname{J}^{\wp} \neq \circledast$ 

Since  $J^{\wp} \neq \bigcirc$ . This contradicts the assumption.

Therefore, the only  $N_{s}^{\,\circ}\text{-open sets}$  are  $\bigcirc$  and  $\circledast.\,(ii)\rightarrow(i)$ 

Let  $\odot$  and  $\circledast$  be the only  $N_s^{\circ}$ -open sets in  $(H, \tau N_s^{\circ})$ .

Suppose  $(H, \tau N_s^{\circ})$  is not an  $N_s^{\circ}$ -hyperconnected space. Then there exist a non empty J is a  $N_s^{\circ}$ -open set such that cl  $N_s^{\circ}$  (J) =  $(\exists N_{so}^{\circ} (intN_s^{\circ}) (P) \neq (\circledast)$ Therefore, we have  $(clN_s^{\circ}) (int N_s^{\circ}) (P) = \bigcirc$  $cl N_s^{\circ} (P) = \bigcirc$  $\therefore P \neq \bigcirc$ 

This contradicts our assumption that (H,  $\tau$  N\_s°) is not an N\_s°-hyperconnected space.

Therefore,  $(H,\tau~N_{s}{}^{\circ})$  must be an  $N_{s}{}^{\circ}\text{-}$  hyperconnected space.

**Theorem 3.8** An  $N_s^{\circ}$ -topological space (H, $\tau$   $N_s^{\circ}$ ) is an  $N_s^{\circ}$ -hyperconnected space if and only if every  $N_s^{\circ}$  subset is either  $N_s^{\circ}$ -Dense or  $N_s^{\circ}$ -NDense.

Proof. Let  $(H, \tau N_s^{\circ})$  is  $N_s^{\circ}$ -hyperconnected space and let J be any  $N_s^{\circ}$  subset then  $J \subseteq \circledast$ .

Assume J is not  $N_s^{\circ}$ -NDense. Then int  $N_s^{\circ}$ ) ((\*)-cl  $N_s^{\circ}$  (J) = (\*) -int  $N_s^{\circ}$  (cl  $N_s^{\circ}$ ) (J)  $\neq$  (\*) Since int  $N_s^{\circ}$  (cl  $N_s^{\circ}$ ) (J))  $\neq$  (·) cl  $N_{so}$  (int  $N_s^{\circ}$  (cl  $N_s^{\circ}$ ) (J) = (\*) cl  $N_s^{\circ}$  (J) = (\*)

Hence J is N<sup>o</sup>-Dense.

Conversely, Let J be any non empty set in  $N_s^{\circ}$  open set. Then  $J \subset int N_s^{\circ} (clN_s^{\circ}) (J))$   $\therefore$  J is not a  $N_s^{\circ}$ -NDense. J is a  $N_s^{\circ}$ -Dense.

**Definition 10** A  $N_s^{\circ}$ -topological space (H, $\tau$   $N_s^{\circ}$ ) is called as  $N_s^{\circ}$  extremely disconnected ( $N_s^{\circ}$ -extremely disconnected) if the  $N_s^{\circ}$ -closure of each  $N_s^{\circ}$ -open set is  $N_s^{\circ}$ -open in (H, $\tau N_s^{\circ}$ ).

**Theorem 3.9** Every  $N_s^{\circ}$ -hyperconnected space is an  $N_s^{\circ}$ -extremely disconnected, in an  $N_s^{\circ}$ -topological space (H, $\tau N_s^{\circ}$ ).

Proof. Let us take  $(H, \tau N_s^{\circ})$  is not  $N_s^{\circ}$ -hyperconnected. be  $N_s^{\circ}$ -hyperconnected. Then for any  $N_s^{\circ}$ -open set P, cl $N_s^{\circ}$ ) (P) = (\*).

 $cIN_{s}^{\circ} (P) \ is \ N_{s}^{\circ} \text{-open. Therefore} \ (H, \\ \tau N_{s}^{\circ}) \ is \ not \ N_{s}^{\circ} \text{-hyperconnected.} \ is \ N_{s}^{\circ} \text{-extremely} \\ disconnected.$ 

**Remark 1** The following example illustrates that the converse of the above theorem does not necessarily hold true.

**Example 2** Let  $\varepsilon = \{e\}$  be a set of parameter on H, where H = {s} with  $\tau N_s^{\circ} = \{\odot, \circledast, P_1, P_2, P_3\}$ .  $P_1 = \{(e, \{s, 1.4, 0.7, 0.2 : s H\}): e \in \varepsilon\}$  $P_1 = \{(e, \{s, 0.2, 0.7, 1.4 : s H\}): e \in \varepsilon\}$  $P1 = \{(e, \{s, 1.1, 0.5, 0.3 : s H\}): e \in \varepsilon\}$  $cl N_s^{\circ}(P_1)\{(e, \{s, 1.4, 0.7, 0.2 : s H\}): e \in \varepsilon\}$  $cl N_s^{\circ}(P_2) = \{(e, \{s, 1.4, 0.7, 0.2 : s H\}): e \in \varepsilon\}$  $cl N_s^{\circ}(P_3) = \{(e, \{s, 1.4, 0.7, 0.2 : s H\}): e \in \varepsilon\}$   $\begin{array}{l} \therefore \ (H,\tau N_s^{\ o}) \ is \ N_s^{\ o}\text{-extremely disconnected.} \\ But \ (H,\ \tau(N_s^{\ o}) \ is \ not \ N_s^{\ o}\text{-hyperconnected space. Since } \\ clN_s^{\ o} \ (P_1), \ cl\ N_s^{\ o} \ (P_2) \ and \ clN_s^{\ o} \ (P_3) \ are \ N_s^{\ o}\text{-open but } \\ not \ N_s^{\ o}\text{-dense.} \end{array}$ 

# Correlation Measure for Neutrosophic Over Soft Set

Definition 11<sup>8</sup> Let  $J = (JN_s^{\circ}), \varepsilon$ ) and  $W = (W N_s^{\circ}), \varepsilon$ ) be a  $N_s^{\circ}$ -set over an non-empty set H, where they are defined as follows:

 $\begin{aligned} \mathsf{J} &= \{(\mathsf{e}, \{ \mathsf{m}, \vartheta_{\mathsf{J}}(\mathsf{m}), \check{\sigma}_{\mathsf{J}}(\mathsf{m}), \gamma_{\mathsf{J}}(\mathsf{m}): \mathsf{m} \in \mathsf{H}\}) : \mathsf{e} \in \varepsilon \} \\ \mathsf{W} &= \{(\mathsf{e}, \{ \mathsf{m}, \vartheta_{\mathsf{W}}(\mathsf{m}), \check{\sigma}_{\mathsf{W}}(\mathsf{m}), \gamma_{\mathsf{W}}(\mathsf{m}): \mathsf{m} \mathsf{H}\}) : \mathsf{e} \in \varepsilon \} \end{aligned}$ 

The correlation coefficients  $\aleph_{_{\rm S}}$  and  $\ddot{Y}_{_{\rm S}}$  between J and W are defined as:

$$\varphi(\mathcal{J}, \mathcal{W}) = \frac{\mathcal{K}(\mathcal{J}, \mathcal{W})}{n(\sqrt{\mathcal{K}(\mathcal{J}, \mathcal{J}), \mathcal{K}(\mathcal{W}, \mathcal{W})})}$$
(1)

$$\varphi^*(\mathcal{J},\mathcal{W}) = \frac{\mathcal{K}(\mathcal{J},\mathcal{W})}{n[\min(\mathcal{K}(\mathcal{J},\mathcal{J}),\mathcal{K}(\mathcal{W},\mathcal{W}))]}$$
(2)

Where

$$\begin{split} \mathsf{K}(\mathsf{J},\mathsf{W}) \, &=\, \sum_{e=1}^{n} ((\vartheta_{\mathsf{J}}(\mathsf{m}_{e}))^{2}.(\vartheta_{\mathsf{W}}(\mathsf{m}_{e}))^{2} \,+\, (\check{\mathsf{O}}_{\mathsf{J}}^{-}(\mathsf{m}_{e}))^{2}. \ (\check{\mathsf{O}}_{\mathsf{W}}^{-}(\mathsf{m}_{e}))^{2} \,+\, (\check{\mathsf{O}}_{\mathsf{J}}^{-}(\mathsf{m}_{e}))^{2}. \ (\check{\mathsf{O}}_{\mathsf{W}}^{-}(\mathsf{m}_{e}))^{2} \,) \end{split}$$

$$\begin{split} & \mathsf{K}(\mathsf{J},\mathsf{J}) = \sum_{e=1}^{n} ((\vartheta_{\mathsf{J}}(\mathsf{m}_{e}))^{2}.(\vartheta_{\mathsf{J}}(\mathsf{m}_{e}))^{2} + (\check{\mathsf{0}}_{\mathsf{J}}(\mathsf{m}_{e}))^{2}.(\check{\mathsf{0}}_{\mathsf{J}}(\mathsf{m}_{e}))^{2} \\ & + (\gamma_{\mathsf{J}}(\mathsf{m}_{e}))^{2}.(\gamma_{\mathsf{J}}(\mathsf{m}_{e}))^{2}) \end{split}$$

$$\begin{split} \mathsf{K}(\mathsf{W},\mathsf{W}) = & \sum_{e=1}^{n} ((\vartheta_{\mathsf{W}}(\mathsf{m}_{e})^{2}.(\vartheta_{\mathsf{W}}(\mathsf{m}_{e})^{2} + (\check{\mathfrak{0}}_{\mathsf{W}}(\mathsf{m}_{e})^{2}.(\check{\mathfrak{0}}_{\mathsf{W}}(\mathsf{m}_{e})^{2},(\check{\mathfrak{0}}_{\mathsf{W}}(\mathsf{m}_{e})^{2})) \end{split}$$

# Flow Chart For Correlation Measure With To Solving N.º-set



# Numerical Illustration Problem Statement

A research committee is evaluating three chemical compounds to determine the most effective one for a new pharmaceutical application. The evaluation is based on multiple criteria including Efficacy, Stability, and Safety. The compounds being evaluated are Ibuprofen, Paracetamol (Acetaminophen) and Aspirin (Acetylsalicylic acid). The committee needs to rank these compounds to decide which one to prioritize for further development.

### **Replacement and Criteria**

We consider three compounds: lbuprofen(I), Paracetamol(P) and Aspirin(A).

Where, molecular structure and formula for the compounds (Source: Adapted from<sup>19</sup>)









#### Fig. 2. Scheme of syntesis of Paracetamol



The required qualities are categorized under three main criteria: Efficacy, Stability, and Safety. The goal is to rank these compounds from best to worst based on their overall performance as Best Compound, Second Best Compound and Worst Compound.

Therefore, the Replacement sets are Compounds, Rank and the Criteria set is Efficacy, Stability, Safety.

# **Analized Data**

 Table 1: Correlation Between Required

 Compounds and Essential Qualities

Х	Efficacy	Stability	Safety
I	(1.3,1.1,0.5)	(0.8,1.5,0.6)	(1.4,0.8,0.8)
Р	(1.2,0.7,0.9)	(1.6,0.7,0.6)	(1.4,0.6,0.3)
А	(1.8,0.7,0.6)	(1.5,0.3,0.8)	(1.6,0.9,0.4)

Table 2: Correlation between Required Qualities and Rank

1.5,0.4) 0.5,0.3)	(0.5, 1.3, 0.6) (1.5, 0.6, 0.7) (1, 1, 0, 7, 0, 4)	(1.5,0.5,0.6) (1.4,0.3,0.7) (0.9,0,8,0,6)
	1.5,0.4) ).5,0.3) ).7,0.8)	1.5,0.4)(0.5,1.3,0.6)0.5,0.3)(1.5,0.6,0.7)0.7,0.8)(1.1,0.7,0.4)

# Table 3: $\aleph_{\rm s}$ Correlation between Compounds and Rank

φΕ	Best Compound	Second Best Compound	Worst Compound
I	0.2529	0.2118	0.2161
Ρ	0.2767	0.3032	0.2961
Α	0.2385	0.2420	0.3155
0 0 0 0 0 0	30 - Best Compound Second Best Worst 22 - 15 - 10 - 05 -		
0.	1	P	A
		Compounds	



φ	Best Compound	Second Best Compound	Worst Compound
I	0.2947	0.2537	0.2547
Ρ	0.3138	0.3535	0.3300
A	0.3527	0.3678	0.4719



Table 5: Summerv

Compounds	Rank	
I	Best Compound	
Р	Second Best Compound	
А	Worst Compound	

Thus the compund I got the most effective one for a new pharmaceutical application.Also, Compound P and A got second best and worst rank.

# DISCUSSION

The results indicate that Ibuprofen is the most effective compound based on the criteria evaluated, followed by Paracetamol and Aspirin. This ranking aligns with existing literature on the efficacy and safety profiles of these compounds.

# CONCLUTION

This paper gives a clear explaination for neutrosophic over soft semi-j open set and neutrosophic over soft hyperconnected space with its basic definitions theorem and suitable example. numerical illustration is given to understand the neutrosophic over soft set concept in a easyway. The application of  $\aleph_s$  and  $\ddot{Y}_s$  correlations provides a robust framework for evaluating pharmaceutical compounds. This method can be extended to other compounds and criteria, offering a versatile tool for pharmaceutical research.

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#### **Conflict of interest**

The authors declare no conflict of interest.

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