



The Double Wall Boron Nitride Nanotube: Nano-Cylindrical Capacitor

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<http://dx.doi.org/10.13005/ojc/330320>

(Received: February 17, 2017; Accepted: March 13, 2017)

ABSTRACT

Experimental results have shown that a small single wall carbon Nanotubes (SWCNTs) can be usually found inside “multi-walled” (MWCNTs). In this work it has been reported the stabilities and electronic structure of the single wall boron nitride Nano-tube (SWBNNTs) inside SWBNNTs. It has been shown that the gap energies and that energy of BNNTs are strongly dependent on their diameters or chirality. When this kind of BNNTs are inserted in the larger one of SWBNNTs, the gap energies of the double walled (DWBNTs) would even be much decreased due to the “coupled effect” of “wall buckling” difference and inter-wall π - π^* “hybridization”. DWBNNTs are used for a theoretical study of a cylindrical molecular capacitor, including an inner cylinder with a positive charge distribution and an outer cylinder with a negative charge distribution. Due to their semiconductor characteristic and dielectric functionalities of SWBNNTs, DWBNNTs can be used as a cylindrical capacitor for the electronic devices.

Keyword: single-wall BN-nanotubes, nano-cylindrical capacitors

INTRODUCTION

NSCCE or “Nanometer-scale capacitive charging effect” currently is familiar, e.g., the “coulomb blockade phenomenon” in the quantum dots^{1,2}. However, they are arduous for resolving the detailed radial charges repartition within the nanostructures. Using SWBNNTs@SWBNNTs double wall tubes; it has been discussed the “radial” charge distributions of multi layered molecular capacitors.

Designing and control of Nano-tubes diameters are requirement to develop Nano-tube

growth method. Nano-tubes with the diameters of less than one nanometer provide the ideal Nano-spaces in X-dimension³. A few years ago, it has been suggested which the sizes of the catalysts used in the metal catalyze CVD (chemical vapor deposition) can explain the diameter of grown carbon nanotube⁴. This opinion has been confirmed by the seeing that a catalytic particle in the end of chemical vapor deposition grown nanotube has size proportional with the Nano-tubes diameters⁵.

Chin Li Cheung, illustrate clearly the concepts of different sizes nano cluster catalysts which they can be used for controlling the structures

and diameters of "CVD" grown nanotubes⁶. Small-diameter carbon nanotubes indicate to many exotic properties such as an-isotropic optical absorption spectra⁷ and super conductivities emanate from a "Pearle" distortion^{8,9}. This finding has stimulated much fondness in studies of a small nanotube in both theoretically and experimentally¹⁰⁻¹⁴. BN-Nanotubes (BNNTs), which firstly synthesized and predicted through Chopra work and Rubio respectively^{15,16}, has a unique structural syllogism to carbon Nano-tubes but, contrary to the C-N-T being semiconductor or metallic depending on their chirality¹⁶. BNNT is usually can be used as an insulator regardless of its diameter and helicity or the number of walls¹⁵⁻¹⁷.

Experimental result has shown that a small SWNT is usually found inside a multi-walled CNT¹¹⁻¹³. Therefore, there are strong incentive for studding in details the stabilities and interaction of narrow BNNT inside a bigger one in viewpoint of diameter, which makes easier for understanding the experimental result. Furthermore, the studies of double-walled boron nitride Nano-tubes (DBNNTs) have displayed interesting variations in its electronic properties comparing with those of free-standing part of BNNTs¹⁸. So it is also significant for seeing the interaction energies associated and inter wall coupling behavior with the narrow BNNTs^{17,18}.

B-Nnanotube possesses grate band gap around 5 to 6 eV regardless of diameters, chirality, electronic properties and the number of walls^{15, 19}. Furthermore, they are stable in view-point of mechanical and chemical structures²⁰. Therefore, narrow single-wall BNNT can widely be applies as an ideal Nano-tube for the Nanosciences for producing suitable material such as; capacitor, atomic wire, and semiconductor^{21, 22}. In our study the SWBNNs are special material as an insulator for producing Nano-cylindrical capacitors²².

Ryo Nakanishi reported an important synthesis method of a narrow SWBNNT having uniform distribution of diameter around 0.7 ± 0.1 nm¹. Their strategies to synthesize thin BNNTs are for combining the Nano-template reaction using Single wall carbon Nano-tubes which has developed in the past ten years²³. In their systems, precursor molecules including Ammonia Borane Complexes or ABC, including boron and nitrogen were

en-capsulated first in the single wall carbon tubes followed by suitable thermal decomposition-fusion²² reaction inside the SWCNTs^{22,23}.

It has been used arc-grown SWCNTs²⁴ with distribution (diameter) around 1.4 nm²⁴ as a model for synthesizing narrow SWBNNT^{22,24}. Those distributions of SWCNT-models are essential for realizing the diameter selective synthesizing of BNNTs.

In this investigation, the systems have been simulated based on the various distribution diameters of SWBNNTs @ SWBNNTs corresponding the experimental results of Ryo Nakanishi results¹. So we have started for answering to some questions for the mechanism of the radial charge distributions on the inner and outer electrodes, band gapes, potential difference²³ between two layers of the Nano cylindrical²⁴ capacitor and the capacitance of our system when the inner tubes are semiconducting²⁵, and the others are metallic²⁶.

Gugang Chen in the studies of doped double-walled carbon nanotubes²⁶ exhibited the Resonant-Raman-Scattering (RRS) from the phonons²⁶ on each carbon shell determines the radial charges distributions²⁶. The self-consistent including tight-binding model (SCTB) confirms²⁵ the observed molecular faraday-cage effects, so most of the charges reside on the outer-walls, even when these walls were originally²⁶ semiconducting and the inner-walls were metallic²⁴⁻²⁶.

Those systems have been modeled as three-layer cylindrical capacitor within bromine anion forming the shell (around the outer nanotubes²⁶). The total energies contain 3 terms including the innertube, outer tube and band structures of the electrostatic energies E^{es} for the three-layer charge distributions: $\sum_{i,k} E_i^{inner}(k) + E_i^{outer}(k) + E_{es}$

The signs "i" and "k" label the wave vector and occupied band for the outer or inner tube²⁶.

They assumed that the surpluses charges on both shells are distributed in the innitely thin-walls at the nuclear radius of those shell^{26, 27}. The resulting electrostatic energies of the triple-walled capacitors are: $E^{es} = 1/2 e^2 L / 2\pi\epsilon_0 n_{inner}^2 I_n(R_{outer}/R_{inner}) + 1/2 e^2 L /$

$2\pi\epsilon_0 n^2 I_n (R_{Br}, R_{inner})$ where $\{\epsilon_0\}$ is the permittivity of free space²⁷, L is the unit-cell length of the outer tubes and (n) is the linear densities of surplus holes for the innertubes.

There are two physical properties acts in concert²⁷ for isolating most of the holes into the outer nanotubes. (1): the gap band of the thinner diameter tubes towards the larger one, so they empty last²⁸. (2) The cylindrical-geometry rather raises the electrostatic potentials in the inner tubes²⁷. Lonely the charges on the inner tubes in the chirality of Zigzag $(n,0)$ of BNNTs are anticipated to have direct band gaps²⁷. On the other side the armchair (n, n) of BNNTs will have indirect band gaps²⁷. Because of its large band gap around 5 eV, experiments²⁸ using BNNT as the conduction-channel²⁹ for field effect transistors²⁹ or FETs showed that BNNT allowed transport through only the valence band²⁸. The other important features about the band gaps of BNNTs are that they are tunable by doping with carbons²⁹, radial deformation³⁰, or by applying the transverses electric fields through the BNNTs so-called giant-stark-effect³¹⁻³³.

Theoretical band structure calculation suggested that "SWBNNT" can either be n-type or p-type semiconductor by controlling the composition of carbon into "SWBNNTs". Carbon impurities on a boron site result in electron carriers while on a nitrogen site result in holecarriers³⁴.

In this study it has been exhibited that the piezo electricity³⁴ for SWBNNTs causes for increasing the capacities of SWBNNTs@SWBNNTs capacitor comparing to SWCNTs@SWCNTs. This phenomenon³⁵ originated from the deformation effects due to the tumbling of the planar hexagonal boron nitride network to produce tubular structures³⁵. It has been exhibited by Nakhmans on that BNNT could be excellent piezoelectric systems³⁶. As instant, piezoelectric constants for variant zigzags of SWBNNT were found for increasing along with the decreasing of the radius in several BNNTs³⁶. Experimentally³⁷, Bai has exhibited that under in situ elastic bending deformation³⁶ or EBD at room temperature high-resolution-transmission-electron-microscope^{36,37}, a normally electrically insulating³⁷ MWNNT may transform to a semiconductor³⁷.

K. Uchida *et al.*,³⁸⁻³⁹ in a discussion of quantum effect in the cylindrical carbon nanotubes capacitor exhibited that the distributions of the accumulated charges in the inner tubes are quantum mechanically³⁷ spilled outward, while that in the outer tubes are penetrating inwards³⁸. They have shown the reflecting those charges spills, the electrostatic capacitance of the systems are larger than what would be expected from the classical theories³⁸.

Finally, they have shown that the capacitance exhibit two principal quantum effects, (1): the capacitance shows a large bias dependence³⁸, reflecting the densities of states of the carbon Nano tube electrodes. (2): the capacitances are enhanced according to a quantum mechanical spill of the stored electrons density from the tubes walls of the CNTs³⁶⁻³⁸.

Based on our previous works⁴⁰⁻⁶¹, we simulated our model in viewpoint of different band gap energies via considering the single wall boron nitrides as both inner and outer tubes with variant diameters and chirality in the ranges of $(6.0 < d < 8.0 \text{ \AA})$ and $(11.0 < d < 16.0 \text{ \AA})$ for inner and outer tubes respectively.

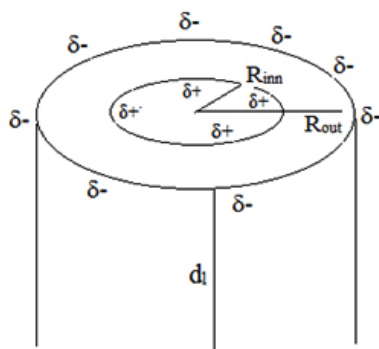
Theoretical background

Carbon nanotube is thin seam less graphitic cylinders³⁹, which exhibit an unusual combination of the Nano-meter size diameter and Milli-meter size length³⁹. These topologies, are included with the absence of defects³⁸ on the macroscopic scales⁶², yields to uncommon electronic properties of individual^{62,63} SWCNTs that depends on their diameters and chirality⁶³, can be either⁶³ insulating, metallic or semiconducting^{64,65}.

Consider a cylindrical capacitor of length " d_l ", inner radius " R_{inn} ", outer radius " R_{out} ", and with charges $Q = d_l q_\lambda$ which q_λ is the charges per unit length (magnitude) on each cylinders (Scheme1). Assume " d_l " \gg " R_{inn} " or " R_{out} " and Neglect fringing and electric elds between cylinders: use Gauss' law $E(2\pi r d_l) = d_l q_\lambda / \epsilon_0 = E(r) = q_\lambda / 2\pi\epsilon_0 r$ (1) and electric potentials between cylinders: use $V_{out} = 0$ $V(r) = -\int_{R_{out}}^r E(r) dr = -\frac{q_\lambda}{2\pi\epsilon_0} \int_0^r \frac{dr}{r} = -\frac{q_\lambda}{2\pi\epsilon_0} \ln \frac{r}{R_{out}}$ (2) And $V = V_+ - V = V_{(inn)} - V_{(out)} = Q/2\pi \epsilon_{oL} \ln R_{out} / R_{inn}$ (3) and capacitances for cylindrical geometries are:

$\bar{C}_g \equiv \frac{Q}{V} = \frac{2\pi\epsilon_0 d_l}{\ln\left(\frac{R_{out}}{R_{inn}}\right)}$ (4) which "K" is the dielectric constant of the system⁸⁵.

$\Delta V_{(inn-out)}$ is positive quantities because $2\kappa \ln(R_{inn}/R_{out})$ is a positive quantities these because outer layers are at a higher potential than the inner layers.



Scheme 1

In our systems the calculation of the nano-cylindrical capacitors can be obtained from the electrical potential in the spaces between two coaxial cylinders of radii R_{inn} and R_{out} and finite length d_l in the z direction, $0 \leq z \leq d_l$. We supposed the geometrical capacitances in our systems are a function of d_l , R_{inn} , R_{out} or $C_g = F(d_l, R_{inn}, R_{out})$. Bilalbegović⁶⁶⁻⁶⁸ with a molecular dynamic simulation and extension series based on Bessel functions⁶⁹ has modified and discussed that capacitance around the shorter coaxial cylinders of radii⁶⁹. So the capacitance in our model can be calculated via $C_g = \frac{2\pi R_{inn}\epsilon_0}{V} \int_0^{d_l} \left(\frac{\partial\phi}{\partial r}\right)_{r=R_{inn}} dz$ (5) in the Finite Nano-meter scales cylindrical-capacitor based on the classical electrodynamic⁸⁵. For calculation the capacitance for the eq.4 and eq.5 for (\bar{C}_g, C_g) the potential difference applied between two cylindrical plates $V = V_{(inn)} - V_{(out)}$ has been calculated by pop = chelp G commands⁷⁶.

Computational details

Calculations were accomplished using GAMESS-US packages⁷². In this work, it has been mainly focused for optimization of each tube with DFT methods⁷³⁻⁷⁷ consist of the m06 and m06-L⁷⁴. The m062x⁷⁴, m06-L⁷⁴, and m06-HF⁷⁴ are a unique Meta hybrid⁷⁴ DFT functional with a good correspondence in non-bonded⁷⁸ calculations and are useful for calculating the energies of the distances between two coaxial cylinders of radii R_{inn} , R_{out} and in the cylindrical capacitor⁷³. The Perdew, Burke and Ernzerh of (PBE)⁷⁵ exchange correlation⁷⁵ (XC) functional^{74,75} of the generalized-gradient-approximations⁹⁵ (GGA) are adopted. The lattice constant has been optimized for the atomic coordinate and has done through the minimization of the total energies. For geometries optimizations, all the internal coordinates were relaxed until the Hellmann-Feynman-forces⁷⁴ was less than 0.005 angstrom.

At each inter tube configurations, a single point calculation is carried out and the total energies are recorded. The resulting sliding rotation energy surface is used for fixing our model in a better position.

We employed DFT theories with the van der Waals DFT for modeling the exchange-correlation energies of SBNNTs and SWCNTs⁷⁶. The $\{\xi$ -basis set⁷⁶ with polarization⁷⁶ orbital was used for single wall tube⁷⁶.

For non-covalent approaches, DFT methods disable for describing van der Waals^{73,77}. The other functional are correctly insufficient for showing the correlation and exchange energies in non-bonded medium-ranges distances. Furthermore, recent study has illustrated that the medium-range exchange^{78,79}

Table1: Gap energy, Fermi level and interaction energy between two layers of DWBNTs

SWBNTs @SWBNTs	LUMO/HOMO Gap(kJ/mol)	Fermi energy level (a.u.)	R_{out}/R_{inn}	$ \Sigma Q $	$\Delta E_s = E_{total} - (E_{inn} + E_{out})$
(5,5)@(7,7)216	7.96	-0.393580	0.85	0.53	-0.44 eV
(5,5)@(8,8)	9.67	-0.393452	0.95	0.89	-0.53 eV
(5,5)@(9,9)	7.55	-0.393364	1.02	0.71	-0.31 eV
(5,5)@(10,10)	8.75	-0.393375	1.08	0.15	-0.22 eV

energies leads to the large systematic errors⁷⁸ in the prediction of molecular properties⁷⁹.

We further calculated the interaction energies between two coaxial cylinders of radii “ R_{inn} ” and “ R_{out} ” for SBNNTs and SWCNs in the structures. The dielectric permittivities as function of dielectric size were determined via

Abinito calculation⁷⁸⁻⁷⁹. The interaction energies for capacitor were calculated via an extended huckel method in all items according to the eq.6. ΔE_s (eV) = $\{E_{total} - (2E_{SWNT} + E_{SWBNNT})\} + E_{BSSE}$ (6) Where the “ ΔE_s ” is the stability energy of capacitor.

The charge transfer and electrostatic potential-derived also calculated using the “Merz-

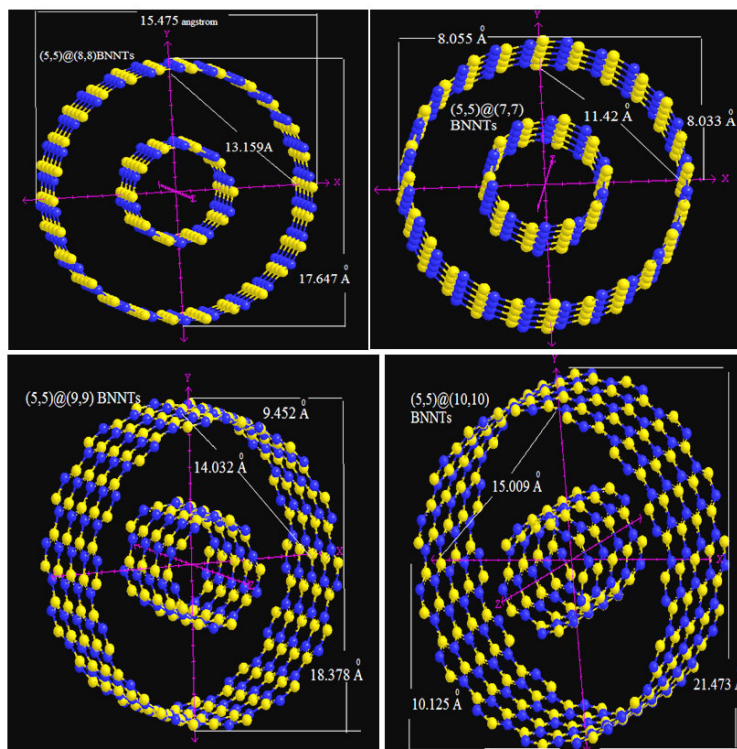


Fig. 1: Dimension of MWBNTs with various diameters and chiralities

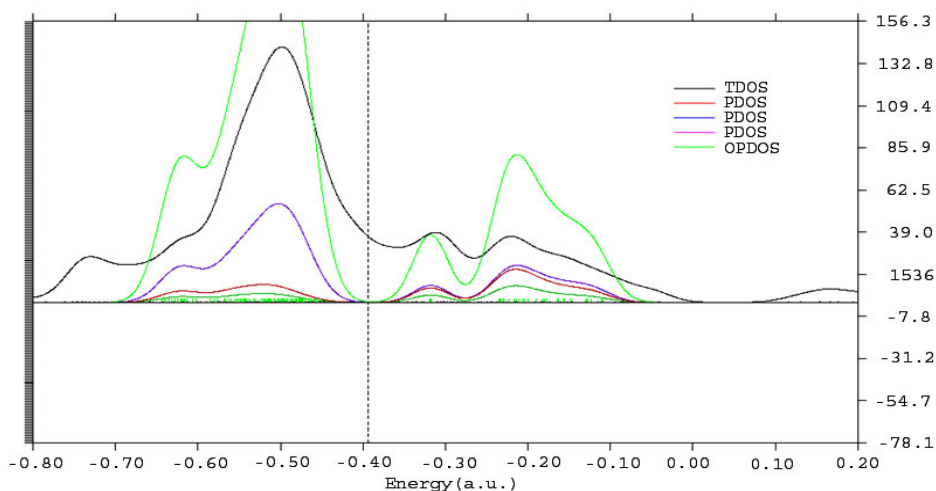


Fig. 2: TDOS, PDOS, OPDOS versus energy for (5,5)@(8,8) BNNTs

Kollman-Singh⁸⁰, Chelp⁸¹, ChelpG⁸² and MESP⁸³⁻⁸⁴.

The MESP's are calculated and distributed at large number of grid points⁸⁴ in a cube regularly.

The representative⁸⁵ atomic charges⁸⁶ would be computed as averages values over a few molecular conformations for the molecules^{86,87}.

The electron densities Both of Laplacian⁸⁸ and Gradient norms⁸⁹, value of orbital wavefunction⁹⁰, electron spin densities⁸⁸, localization function (ELF)⁸⁹, localized orbital locator⁹⁰, electrostatic potential⁸⁸ from nuclear- atomic-charges, electron total electrostatic potential (ESP)⁹⁰, and the exchange-correlation density, correlation hole and correlation factor, Average local ionization energy using the Multifunctional-Wave-function Analyzer⁸⁸⁻⁹⁰.

RESULT AND DISCUSSION

We first consider the h-BN sheet and 3D BN tubes in various diameters and chirality where the (5, 5) @ (8, 8) structure is found as a stable form compared to other forms. The stability depends on the distance between inner radius " R_{inn} ", and outer radius " R_{out} " in one hand and the chirality on other hand Table1. The minimum energies are calculated based on eq.9 in terms of the total energy of the optimized structures and are listed in Table1.

The differences in the band structure and Fermi⁸⁸ level energy of different tubes have been calculated. Furthermore, we have presented the

number of states in unit energy interval through density of states (DOS) (Fig.1). DOS⁸⁸ was plotted as a curved map and we have considered those graphs as a tool for analyzing the nature of electronic structure in our systems^{88,89}. The original total DOS (TDOS)⁸⁹ of our system was calculated based on References {108-110}¹⁰⁸⁻¹¹⁰ in Figs. 2, 3, 4 and 5.

The interaction energies for capacitors were calculated in all items according to the eq. 6 ΔE_s (eV) = $\{E_c - (2E_{Dopant-G} + E_n - E_{BN})\} + E_{BSSSE}$ Where the " ΔE_s " is the stability energy of capacitor.

The wall buckling has been defined as the differences between the mean radiuses⁹¹ of the cylinders consisting of the B and N atoms. It has been shown that the buckling rapidly increases⁹² with decreasing of the tube diameter⁹¹ and are independent of the chirality^{92,93}.

The (5,5) SWBNNTs in the form of inner cylindrical are semiconductors due to the existence of an energy gap in the range of (7.55-9.67) KJ/mol (Table1) which are between the valence band and the conductor⁹³ band. Those armchair tubes have a direct band gap, similar to the BN structure⁹⁴.

The projected local density of states (PDOS) of B and N are plotted in Fig.2 together with the total DOS for comparison. The data for interaction energy shows that the (5, 5) @ (8, 8) DWBNNTs have a stable form comparing to other systems which yields a suitable charge transfer for the Nano capacitor^{92,93}.

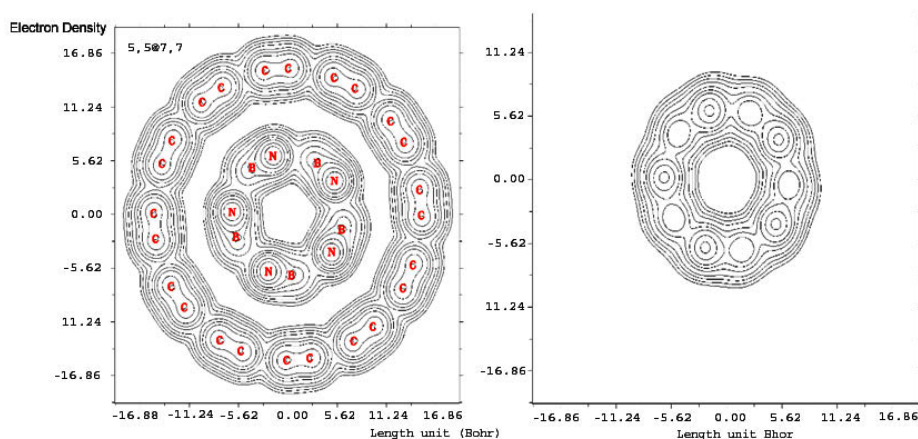


Fig. 3: Counter maps of density for (5,5)@(7,7) BNNTs

The calculated values of charge transfer for (5, 5)B-N-NTs @ (7, 7)B-N-NTs, (5,5)B-N-NTs @ (8, 8)B-N-NTs and (5, 5)B-N-NTs @ (9, 9)B-N-NTs and (5, 5)B-N-NTs @ (10, 10)B-N-NTs from inner to outer tubes is found to be 0.53, 0.89, and 0.71 and

0.15 electrons respectively, which is an acceptable value (Table1) and it is small for the (5, 5) @ (10, 10) structures due to their unstable forms (Fig 3).

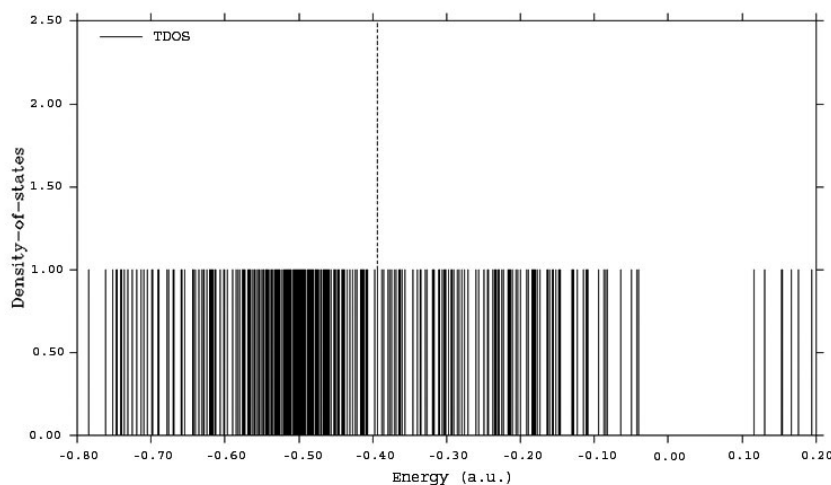


Fig. 4: Density of State versus energy for (5,5)@(8,8) BNNTs

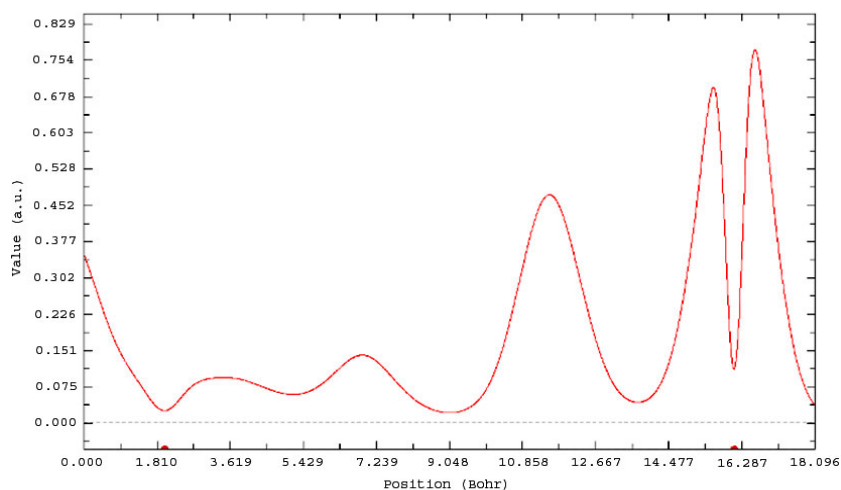


Fig. 5: Energy versus position (Bohr)

Table2. The dielectric constant and C_g for various DWBNTs

SWBNTs @ SWBNTs	$I_n R_{out}/R_{inn}$	$ \Sigma Q $	$\sum_{-V_1}^{V_2} V_2$	$C_q \times 10^{20}$	$\frac{2\pi\epsilon_0 d_l}{\ln \frac{R_{out}}{R_{inn}}} = \bar{C}_g \times 10^{20}$	$k = \frac{\bar{C}_g}{C_q}$
(5,5)@(7,7)	0.85	0.53	1.23	6.8	9.8	1.44
(5,5)@(8,8)	0.95	0.89	1.65	8.63	8.77	1,016
(5,5)@(9,9)	1.02	0.71	1.43	7.94	8.17	1.029
(5,5)@(10,10)	1.08	0.15	0.78	3.07	-	-

It is indicated in this study that the DWBNNTs can be used as a capacitor due to the semiconductor character, metallic behavior and dielectric function of SWBNNTs. Surprisingly, the optical properties⁹³ of the SWBNNTs optimized by Guo⁹⁴ found that the dielectric function⁹³ could also be divided into two spectral regions⁹⁴, namely, the high and the low energy region -energies these systems⁹⁴.

We show that for the (5, 5) @ (8, 8) the distribution of the accumulated charges in the inner tubes are quantum-mechanically spilled outwards clearly. The capacitance (C_q and C_g) and dielectric

constant of the various capacitors have been calculated based eq.4 and are listed in table. 2.

CONCLUSION

This work has been investigated the electric polarization and capacitance in a nano-scale coaxial-cylindrical-capacitors which is made of DW boron nitride, (n, n) @ (m, m), using ONIOM model including density-functional and semi empirical methods with the enforced Fermi-energies difference scheme. Despite the fact that the SWBNNTs@SWBNNTs are a cylindrical capacitor, it has a very sensitive electrical storage compared to SWCNTs@SWCNTs.

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